

# pdfquiz – a T<sub>E</sub>X CAA system

(Udo Hertrich-Jeromin, 13 September 2006)

**Original Problem:** Create maths quizzes for M11 students.

**Ultimate Hope:** Reduce (exam) marking load for large courses.

**Achievements (M11, Spring 06):**

- Quizzes for students to practice (as part of homework sheets).
- Improved average exam marks (is this related?).
- Reduced homework marking load.

**Remaining Problems:**

- Can quizzes replace exams?
- How to operate assessed quizzes?
- How to design intelligent questions?

## Examples: Multiple response and numerical questions

### Problem 2.1

Tick the statements that you think are correct, or fill in the correct number.

- (i) If a subset  $A \subset \mathbb{R}$  has the property that  $\forall x \in A \exists \eta > 0 : (x - \eta, x + \eta) \subset A$ , then  $A$  is an open interval.
- (ii) Let  $f, g : [a, b] \rightarrow \mathbb{R}$  be continuous. If  $f(a) < g(a)$  and  $f(b) > g(b)$ , then there exists  $z \in (a, b)$  such that  $f(z) = g(z)$ .
- (iii) The polynomial  $f(x) = x^5 - 5x^4 + 2x + 1$  has at least two distinct roots in the interval  $[-1, 1]$ . (Hint).
- (iv) Follow the procedure in the proof of the IVT in order to determine the zero of  $f : [-1, 1] \rightarrow \mathbb{R}$ ,  $f(x) := (4x)^3 - 16x + 1$ , up to an accuracy of  $\frac{1}{16} = 2 * 2^{-5} = 0.0625$ :  $f$  has a zero in the interval  $(x - \frac{1}{16}, x + \frac{1}{16})$ , where  $x =$  (input the center of the interval in decimal format).
- (v) The zero approximated in (iv) is the only zero of the function in the interval  $(-1, 1)$ .

Evaluate

## Examples: Multiple response and numerical questions

### Solution.

(i) This statement is false. Take for example  $A = (0, 1) \cup (2, 3)$ . Then it is easy to check that  $A$  has the above property, but obviously  $A$  is not an interval.

(ii) This is a true statement. Let  $h : [a, b] \rightarrow \mathbb{R}$  be given by  $h = f - g$ . Then  $h$  is continuous,  $h(a) < 0$  and  $h(b) > 0$ , hence by the IVT there exists  $z \in (a, b)$  with  $h(z) = 0$ , i.e.  $f(z) = g(z)$ .

(iii) This statement is true. Clearly  $f$  is continuous on  $[-1, 1]$ . Now  $f(-1) = -9$ ,  $f(0) = 1$  and  $f(1) = 1$ , so by the IVT  $f$  has a root on  $(-1, 0)$ , and another root on  $(0, 1)$ .

(iv) Following the procedure in the proof of the IVT: our starting interval is  $[-1, 1]$ : we have  $f(-1) = -3 * 16 + 1 < 0$ ,  $f(1) = 3 * 16 + 1 > 0$  so that there must be a zero of  $f$  in  $(-1, 1)$  by the IVT; now we follow the proof:

check  $f(0) = 1 > 0$ , hence a zero in  $(-1, 0)$ ,

check  $f(-\frac{1}{2}) = -2^3 + 8 + 1 > 0$ , hence a zero in  $(-1, -\frac{1}{2})$ ,

check  $f(-\frac{3}{4}) = -3^3 + 12 + 1 < 0$ , hence a zero in  $(-\frac{3}{4}, -\frac{1}{2})$

check  $f(-\frac{5}{8}) = \frac{-125+88}{11} < 0$ , hence a zero in  $(-\frac{5}{8}, -\frac{1}{2}) = (-\frac{10}{16}, -\frac{8}{16})$ ,

i.e.,  $x = -\frac{9}{16} = -0.5625$ . (Any  $x$  in the interval  $(-\frac{10}{16}, -\frac{8}{16})$  is considered correct.)

(v) Check  $f(\frac{1}{4}) = -2 < 0$ : by the IVT  $f$  has two more zeroes, in  $(0, \frac{1}{4})$  and in  $(\frac{1}{4}, 1)$ .

## Examples: Multiple response, different flavour

### Problem 8.3

All of the following functions have a differentiable extension to all of  $\mathbb{R}$  (make sure that you understand why!). For each function tick the properties you think it has:

$$x \mapsto x^2 \quad x \mapsto x^2 \left(1 - \sin \frac{1}{x}\right) \quad x \mapsto \frac{\sin x}{x} \quad x \mapsto \frac{1 - \cos x}{x}$$

$x = 0$  is a critical point

0 is a local extremum

0 is an extremum

monotone on  $(0, \infty)$

monotone on some  $(0, \delta)$

And, finally, the question: is there a differentiable function  $f : \mathbb{R} \rightarrow \mathbb{R}$ , which has a strict minimum at  $x = 0$ , is strictly decreasing on  $(-\infty, 0)$  but not increasing on any interval  $(0, \delta)$ ,  $\delta > 0$ ?

Evaluate

## Design goals

- Simplicity (concentrate on maths, not technicalities)
  - easy for lecturer to design quizzes
  - easy for student to understand the operation
- Flexibility and Portability (use it in different contexts)
  - online/offline operation
  - separation of functionality and layout
  - independence of T<sub>E</sub>X dialect
- Adaptability (adapt/extend functionality as needed)
  - Open source
  - Clear and easy to understand source code
  - Good technical manuals (PDF & Acrobat JavaScript)

## Required Software

- T<sub>E</sub>X, LaT<sub>E</sub>X: pdf[la]tex (other pdf drivers possible but not implemented)
- PDF viewer: Acrobat Reader, v5 or higher (viewer needs to understand JavaScript)
- server side: perl or cgi script (optional)

## New TEX commands

`\qtick[mu:tu;mc:tc]{app}` — creates a checkbox with appearance `app`; `mu/mc` are the marks awarded when the box is unchecked/checked and `tu/tc` is the corresponding text shown after evaluation.

*Example:* `\qtick[3:not checked;-2:box is checked]{\bigcirc}` creates the following check box: .

`\qnuml[mi:ti;mo:to]X(\Delta)` — creates a number input field; `mi/mo` are the marks awarded if the provided decimal is in/not in  $[X - \Delta, X + \Delta]$  and `ti/to` is the corresponding text shown after evaluation.

*Example:* `(\qnuml[0.5:in interval;1:not in interval]1.3(0.2))` creates the following number input field between the parentheses: (  ).

`\qhint[pm:ht]{app}` — creates a hint with appearance `app`; `pm` are the penalty marks for requesting the hint and `ht` is the text of the hint, shown in a pop up box.

*Example:* `\qhint[0.1:this is a hint]{Hint}` produces: Hint.

`\qeval{app}` — creates a button for evaluation with appearance `app`.

*Example:* `\underbar{\qeval{Evaluate}}` creates: Evaluate; click on it to evaluate the boxes in the above examples.

*Remark:* the mark and hint texts are not TEX formatted and should be kept simple.

## New TEX commands

`\qtext(wd,ht) [id]{dt}` & `\qline(wd) [id]{dt}` — provide text input fields (for example, for a feedback form); `wd/ht` specify the width/height of the text box (only width in case of the `\qline` command), `dt` specifies a default text to be shown and `id` specifies the name (`id`) of the text field for reference by the `\qsend` command.

*Example:* `\underbar{\qline(20em) [feedback]{Your feedback}}` creates the following text input line: \_\_\_\_\_.

`\qsend[url;fld]{app}` — creates a button with appearance `app` for submission of the named fields `fld` to a cgi or perl script with URL `url` on a web server.

*Example:* `\qsend[\url;"feedback","qtotal"]{submit}`, where we let for example `\edef\url{http://www.maths.bath.ac.uk/\string~masuh/cgi-bin/quiz.pl}`, produces: submit.

*Remark:* a predefined field “qtotal” holds an array containing (1) the minutes since opening the document, (2) the maximally available marks, (3) the total marks from all evaluations, (4) the total penalties for requesting hints.

`\qsave{app}` — creates a button with appearance `app` to save the results of all evaluations.

*Example:* `\qsave{Save results}` will create: Save results.

*Remark:* The `\qsend` and `\qsave` commands have not been tested properly and may not work as intended.

## New TEX variables

*Counters:* `\qprbno`, `\qoptno`, `\qnumlno` — these count the problem (a new problem starts after each evaluation) and, in each problem, the checkboxes and number input fields, respectively.

*Usage:* These counters can be used to automatically number problems or checkboxes within problems; internally these counters are used to identify checkboxes and numerical input fields — therefore these counters should not be tampered with.

*Dimensions:* `\qmarkwd`, `\qmarkht`, `\qmarkho`, `\qmarkvo` — these control the size (width and height) and offset (horizontal and vertical) of the box containing the mark and comment for each checkbox or number input box.

*Usage:* In order to change the global appearance, change the default values of these dimensions at the beginning of the file; in order to alter the size or position of an individual box, put the new dimensions followed by the corresponding `\qtick` or `\qnuml` command in a group.

*Thank you!*

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